

# A Modeling Framework for Analyzing European Balancing Markets

Anthony Papavasiliou, Gilles Bertrand  
CORE, UCLouvain

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Balancing capacity  $\leftrightarrow$  day-ahead / forward reserve capacity

Balancing energy  $\leftrightarrow$  real-time energy

aFRR, mFRR  $\leftrightarrow$  operating reserves (resources with a response time of seconds to minutes)

- Important EU-wide balancing market integration initiatives
- Functional separation:
  - TSOs: forward procurement of reserve capacity, deployment of reserve capacity in real time
  - NEMOs: operation of day-ahead and intraday market
- **Balancing Responsible Parties (BRPs)**: *price-inelastic* buyers or sellers of real-time energy
- **Balancing Service Providers (BSPs)**: *price-elastic* suppliers or consumers of real-time energy
  - BSPs commit to bidding at least DA reserve capacity to RT balancing markets
  - Each BSP must be attributed to at least one BRP portfolio, according to EU law (EBGL)
- BRPs and BSPs face a different price for real-time energy:
  - BRPs: **imbalance price**
  - BSPs: **balancing price**

- Accurate valuation of energy and reserve capacity is an increasingly crucial function of RT markets in a regime of large-scale renewable energy integration
- **Operating reserve demand curves (ORDCs)** [Hogan, 2005]: means for achieving this goal
  - ORDC adders computed on basis of available reserve capacity in the system
  - When reserve capacity decreases, ORDC adders increase (value of reserve in tight system)
  - When reserve capacity increases, ORDC adders dissipate

# Scarcity Pricing Evolutions Internationally

- ORDC adders have been adopted in Texas
- Adoption of ORDCs is moving forward in PJM
- European Commission Electricity Balancing Guideline article 44(3)

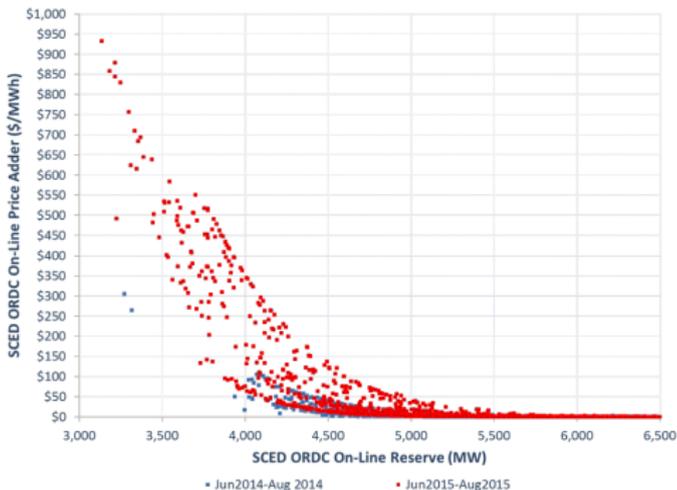
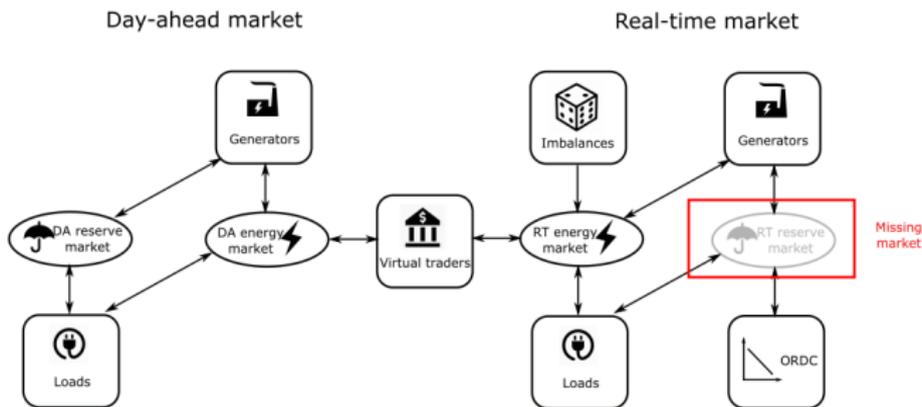


Figure: ORDC adders in Texas, 2014-2015

- Preliminary analyses [Papavasiliou, 2017], [Papavasiliou, 2018] focused on quantifying possible implications of mechanism for reserve resources
- Belgian system operator [ELIA, 2018] publishes scarcity adders based on the “available reserve capacity” (ARC) of the system
- Since October 2019, ELIA publishes scarcity prices for information purposes
  - Computed for every quarter of the day
  - Published one day after operations
- ELIA public consultation on scarcity pricing [ELIA, 2020]

# Translating First Principles to the EU Design

- ORDC essentially sets a RT price for reserve
- In equilibrium, energy and reserve prices follow each other in lock step



So **what does it mean to introduce ORDC adders to the EU market**, if we do not have a RT market for reserve?

- Adders to the imbalance price (BRPs)?
- Adders to the balancing price (also BSPs)?
- What about RT reserve *capacity*?

# Our Proposal for Implementing Scarcity Pricing

- **Proposal 1:** introduction of a scarcity adder to the imbalance price
- **Proposal 2:** application of same adder to the balancing energy price
- **Proposal 3:** implement a real-time market for reserve capacity (equivalently, market for reserve imbalances, in the same way that we operate a market for energy imbalances)

- Rationale of our proposal:
  - **Law of one price** [Cramton, 2006] applied to real-time energy
  - **Back-propagation** of reserve value: If we put in place a real-time market for reserve capacity, agents will only sell reserve capacity in forward markets at the value that they would need to buy it back in real time
- Stochastic equilibrium [Papavasiliou, 2020]
  - Can be used to understand effect of certain market design choices on back-propagation ...
  - ... but it embeds the law of one price as an *assumption*

- Our approach in this work: represent balancing market as a Markov Decision Process (MDP)
- Growing body of work in this direction
  - Early work: analysis of design changes on English and Welsh markets [Bower, 2001], [Bunn, 2001]
  - Application of Q-learning [Naduri, 2007], [Yu, 2010]
  - Deep learning [Ye, 2019], [Ye, 2020]

# A Caveat About MDP Models

- MDP framework: powerful modeling flexibility ...
- ... but difficult to extract generalizable conclusions
- We supplement our MDP-based market simulation framework with analytical results under **perfect competition**

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We consider a *general* agent participating in the balancing market as one which owns

- 1 Uncontrollable assets
- 2 Controllable assets (reserves)
  - marginal cost  $C$
  - upward capacity  $P^+$
  - downward capacity  $P^-$

- Agent that decides how much balancing energy  $q$  to offer to a **uniform price auction** with constant price  $\lambda^B$ 
  - Action of the agent: quantity  $q$ :
  - Reward:  $(\lambda^B - C) \cdot q$ , with  $qa$  the matched quantity
- Agent submitting price-quantity pairs
  - Action space:  $(p, q)$ , i.e. offer of  $q$  MW at  $p$  €/MWh
  - If bids of competitors are fixed, this implies a balancing price
  - Reward of the agent:  $(\lambda^B - C) \cdot qa$
- System-level uncertain imbalance  $\Rightarrow$  uncertainty in balancing price

Belgium applies a surcharge  $\alpha^U$  whenever the system is short, or a discount  $\alpha^L$  whenever the system is long:

$$\lambda^I = \lambda^B + \alpha$$
$$\alpha \triangleq \alpha^U \cdot \mathbb{I}[Imb^t > UI] - \alpha^L \cdot \mathbb{I}[Imb^t < LI]$$

Notation:

- $\lambda^I$ : imbalance price
- $Imb^t$ : total imbalance of the system
- $UI$  and  $LI$ : upper and lower imbalance thresholds at which the surcharge or discount apply, respectively

Actual formula used in Belgium is more complex in practice (accounted for in simulations)

# Two-Stage MDPs: Stage 1

Agent submits a price-quantity bid in the balancing platform

TSO observes the system imbalance, activates BSPs, produces a uniform clearing price



Agent observes imbalance  $Imb$  within its portfolio, decides how much of it to cover

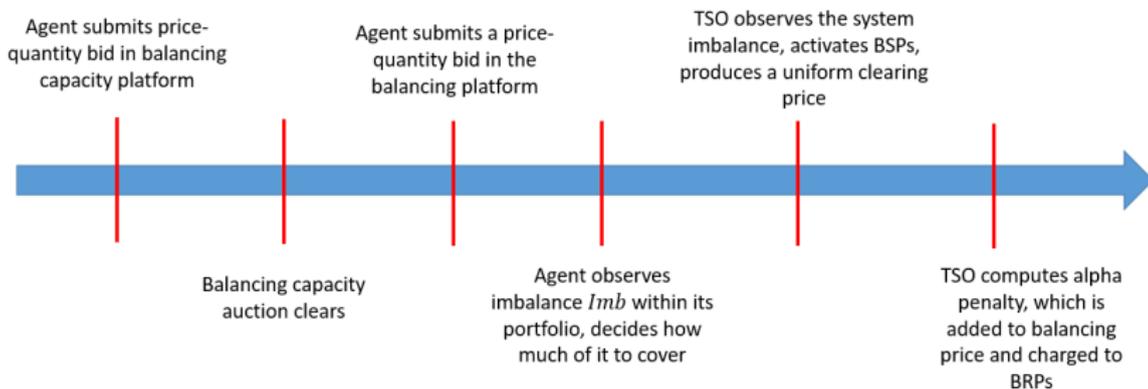
TSO computes alpha penalty, which is added to balancing price and charged to BRPs

- Action:  $(p, q)$ , price-quantity offer in balancing platform
- No reward is collected at this stage.

# Two-Stage MDPs: Stage 2

- State:
  - 1 bid price  $p$
  - 2 leftover BSP capacity after some capacity has been offered to the balancing auction
  - 3 imbalance  $Imb$  of an agent
- Action: How much of the imbalance  $Imb$  to cover (“active imbalance”, must be limited to leftover capacity that BSP has not allocated to reserve auction)
- Reward:
  - 1 BSP payment for upward/downward activation,  $\lambda^B \cdot qa$
  - 2 BRP payment for imbalance settlement,  $-\lambda^I \cdot (Imb - ai)$
  - 3 fuel costs related to self-balancing and BSP activation,  $-C \cdot (ai + qa)$

# Three-Stage MDPs: Stage 1



- Stage 1

- Action:  $(p^R, q^R)$ , price-quantity offer in balancing capacity auction
- Rewards: payment from balancing capacity auction

# Three-Stage MDPs: Stages 2, 3

- Stage 2
  - State: capacity  $qa^R$  awarded in balancing capacity auction
  - Action:  $(p, q)$ , the price-quantity offers in balancing platform, with  $q \geq qa^R$
- Stage 3: identical to stage 2 of two-stage MDP

- **Option D1:** vanilla balancing market design

$$\lambda^B \cdot qa - \lambda^B \cdot (Imb - ai) - C \cdot (qa + ai)$$

- **Option D2:** imbalance price adders (current Belgian market)

$$\lambda^I = \lambda^B + \alpha$$

- **Option D3:** Scarcity adders limited to imbalance prices [ELIA, 2020]

$$\lambda^I = \lambda^B + \lambda^R$$

- **Option D4:** Real-time market for balancing capacity

$$\begin{aligned} & (\lambda^B + \lambda^R) \cdot qa - (\lambda^B + \lambda^R) \cdot (Imb - ai) - C \cdot (qa + ai) \\ & + \lambda^R \cdot (P^+ - qa - ai) - \lambda^R \cdot qa^R \end{aligned}$$

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**Perfect competition assumption:** We consider fringe agents, i.e. ones with infinitesimal capacity who do not influence price outcomes

Rationale of assumption:

- 1 Unveiling difficulties in back-propagating reserve prices in the case of perfect competition suggests *fundamental market design problems*
- 2 Analytical results from perfect competition assumption allow better understanding / interpretation of MDP results

- 1 It is optimal for agents to bid their entire balancing capacity at the true marginal cost to the balancing auction
- 2 For agents with upward balancing capacity ( $P^+ > 0$ ), the opportunity cost of bidding their capacity to the day-ahead reserve auction is zero
- 3 This is a pure strategy Nash equilibrium

# Statement of Analytical Results: D2

- 1 Under the assumption of independent symmetric imbalances, it is optimal for agents to bid their entire balancing capacity at the true marginal cost to the balancing auction
- 2 For agents with upward balancing capacity ( $P^+ > 0$ ), the opportunity cost of bidding their capacity to the day-ahead reserve auction is zero
- 3 This is a pure strategy Nash equilibrium

# Statement of Analytical Results: D3

- 1 For sufficiently high-cost agents, is it optimal for agents for them to bid their entire balancing capacity at the true marginal cost to the balancing auction
- 2 For agents with upward balancing capacity ( $P^+ > 0$ ), the opportunity cost of bidding their capacity to the day-ahead reserve auction is less than or equal to the scarcity value  $\mathbb{E}[\lambda^R]$
- 3 This does *not* characterize a pure strategy Nash equilibrium, since some agents find it optimal to self-balance

D3 depresses scarcity price in two ways:

- 1 Agents who find it optimal to bid their entire capacity to the balancing auction face an opportunity cost of zero for bidding reserve in the day ahead
- 2 Agents who self-balance depress balancing energy prices

# Statement of Analytical Results: D4

- 1 It is optimal for agents to bid their entire balancing capacity at the true marginal cost to the balancing auction
- 2 For agents with upward balancing capacity ( $P^+ > 0$ ), the opportunity cost of bidding their capacity to the day-ahead reserve auction is the scarcity value  $\mathbb{E}[\lambda^R]$
- 3 This is a pure strategy Nash equilibrium

Among the analyzed options, (D4) is the only option which

- back-propagates the real-time value of reserve capacity to day-ahead reserve auctions, while
- preserving the incentive of agents to make their balancing capacity available in the balancing market

- Without loss of generality, consider agent which only has downward capacity (i.e.  $P^+ = 0$  and  $P^- < 0$ ) or only upward capacity (i.e.  $P^- = 0$  and  $P^+ > 0$ )
- Fringe assumption implication: no influence of imbalance on expected imbalance price  $\Rightarrow D \triangleq -\mathbb{E}[\lambda^B \cdot Imb]$  is a constant offset to the imbalance payoff of the agent
- Two possible suppliers:
  - Cheap:  $\mathbb{E}[\lambda^B] \geq C$
  - Expensive:  $\mathbb{E}[\lambda^B] < C$
- In what follows, we focus on cheap suppliers with upward capacity ( $\mathbb{E}[\lambda^B] - C \geq 0, P^+ > 0, P^- = 0$ )

Imbalance payoff:

$$\max_{ai} (\mathbb{E}[\lambda^B] - C) \cdot ai - \mathbb{E}[\lambda^B \cdot Imb]$$

$$ai + q \leq P^+$$

$$ai \geq 0$$

We have  $ai^* = P^+ - q$ , expected payoff  $z_I$  is:

$$z_I = (\mathbb{E}[\lambda^B] - C) \cdot (P^+ - q) + D$$

## Proof for (D1): Balancing Market Payoff $z_B$

Balancing payoff  $z_B(\omega)$ :

- Out of the money: if  $p > \lambda^B$ , then  $z_B(\omega) = 0$
- At the money: if  $p = \lambda^B$ , then  $z_B(\omega) = (\lambda^B - C) \cdot qa$  for some  $qa$  which selected by the auctioneer; use fringe assumption to set  $qa = 0$  and  $z_B = 0$
- In the money: if  $p < \lambda^B$ , then  $z_B(\omega) = (\lambda^B - C) \cdot q$
  
- Balancing payoff  $z_B(\omega)$  is random, depends on system imbalance
- Denote probability measure of balancing price  $\lambda^B$  as  $\mu$
- Expected balancing market payoff:

$$\begin{aligned} z_B &= \mathbb{E}[z_B(\omega)] \\ &= \int_{x > p} (x - C) \cdot q \cdot d\mu(x) \end{aligned}$$

# Proof for (D1): Optimal Balancing Market Price $p$

Overall agent payoff:

$$\begin{aligned} R(p, q) &= z_I + z_B \\ &= C_1 - C_2 \cdot q + C_3(p) \cdot q \end{aligned}$$

where:

$$\begin{aligned} C_1 &= (\mathbb{E}[\lambda^B] - C) \cdot P^+ + D \\ C_2 &= \mathbb{E}[\lambda^B] - C \\ C_3(p) &= \int_{x>p} (x - C) \cdot d\mu(x) \end{aligned}$$

For given balancing quantity bid  $q$ , first-order conditions with respect to  $p$  are:

$$\begin{aligned} \frac{\partial R(p, q)}{\partial p} &= C'_3(p) \cdot q \\ &= -\mu(p) \cdot (p - C) \cdot q \end{aligned}$$

Payoff function  $R(p, q)$  for fixed  $q$  is

- increasing in  $(-\infty, C]$
- zero at  $C$
- decreasing in  $[C, +\infty)$

Thus, for any  $q$ , an optimal strategy is to bid the true cost, which implies

$$R(C, q) = C_1 - C_2 \cdot q + C_3(C) \cdot q$$

# Proof for (D1): Optimal Balancing Market Quantity $q$

First-order conditions with respect to  $q$ :

$$\begin{aligned}\frac{\partial R(C, q)}{\partial q} &= -C_2 + C_3(C) \\ &= -(\mathbb{E}[\lambda^B] - C) + C_3(C) \\ &= -\left(\int_{x \leq C} (x - C) \cdot d\mu(x) + \int_{x > C} (x - C) \cdot d\mu(x)\right) \\ &\quad + \int_{x > C} (x - C) \cdot d\mu(x) \\ &> 0\end{aligned}$$

Therefore, it is optimal to bid  $q^* = P^+$  in the balancing auction, and  $ai^* = 0$

# Proof for (D1): Optimal Balancing Market Quantity $q$

- When being in active imbalance, agent takes risk of producing power when being out of the money
- Instead, balancing market will only activate agent when its marginal cost is lower than the balancing price
- When the balancing and imbalance price are equal, the agent has the incentive to bid its entire capacity to the balancing auction

- Every MW cleared in a forward reserve auction comes with an obligation to bid that MW in the balancing auction
- This is profit lost in the balancing and imbalance phase
- Since the optimal strategy of the agent is to anyways bid its entire capacity in the balancing auction, there is no opportunity cost for the agent, i.e.  $dR^*/dq = 0$

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- Fringe supplier
  - Fringe supplier:  $P^+ = 1$  MW,  $P^- = 0$  MW
  - Marginal cost:  $C = 50$  €/MWh
  - Balancing auction bid  $q$  and reserve auction bid  $q^R$  is either 0 MW or 1 MW
  - Agent can bid any value  $p$  between 25 to 75 €/MWh, in increments of 5 €/MWh
- Imbalances:
  - System imbalance  $\sim N(0, 91.5)$
  - Fringe agent imbalance:  $\sim N(0, 0.41)$
- Balancing supply function:
  - $a + b \cdot q$ , with  $a = 50$  €/MWh, and  $b = 0.11$  (€/MWh)/MW
  - Approximation (for analytical solution purposes) of a balancing market with 8 agents (see next slide)

We validate our analytical results using the MDP model

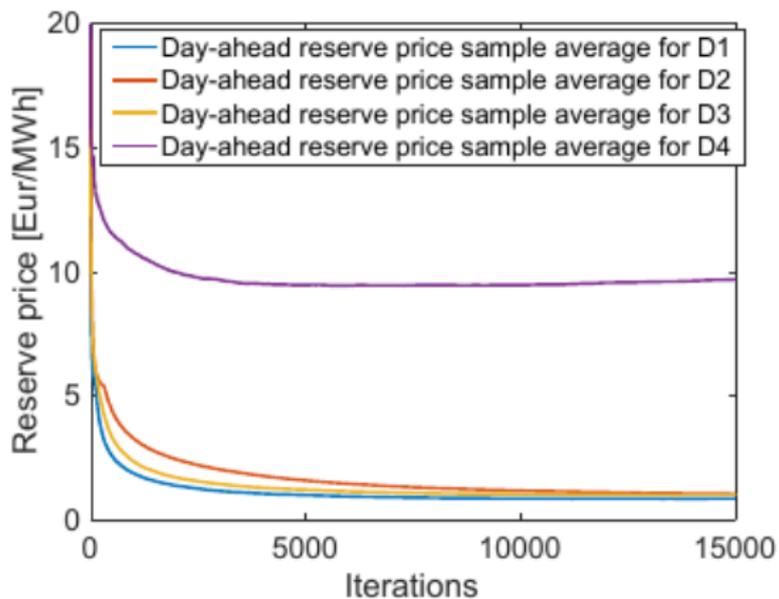
- We assume a fringe agent
- We validate all designs
- See appendix for detailed assumptions of validation study

- Discretize agent action space by having agents bid in price increments of 5 €/MWh and in quantity increments of half of their capacity
- Each agent is facing a portfolio imbalance which is uniformly distributed between zero and half of its capacity
- System imbalance: zero mean and standard deviation of 21.9 MW
- Agent imbalances are independent of each other and system imbalance
- Day-ahead reserve demand curve identical to real-time reserve demand curve

# Multi-Agent Learning Settings

- Q-learning algorithm using  $\epsilon$ -greedy policy, with  $\epsilon_k$  evolving as  $\frac{0.05}{N-k}$
- All agents are learning simultaneously  $\Rightarrow$  no convergence guarantees
- We run 1,500,000 iterations in blocks of 100
- After each block of 100 iterations, we compute the outcome that we would have obtained in the reserve market if each agent were applying its policy greedily

# Multi-Agent Results



- For ( $D3$ ), the reserve price sample average arrives slightly above the one resulting from ( $D1$ ): certain low-cost producers may face a positive opportunity cost when bidding into the day-ahead reserve market
- Under design ( $D4$ ), the day-ahead reserve price converges to a value which is close to the average real-time scarcity adder, i.e. 9.4 €/MWh

# Conclusions and Perspectives

## Conclusions:

- MDP is an interesting framework for analyzing market design options, when supplemented by analytical results
- A market for balancing capacity imbalances can
  - ① back-propagate the value of reserve capacity to forward reserve markets
  - ② while also preserving incentive of agents to offer their capacity in the balancing market

## Perspectives:

- Collaboration with CREG on calibration of ORDC to Belgian system needs
- Discussions with ELIA on scarcity pricing proposal [ELIA, 2020]
- Address questions of market stakeholders on public consultation of ELIA
- Further clarify interaction of market design proposal with EU legislation

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# Thank You for Your Attention

For more information:

- [anthony.papavasiliou@uclouvain.be](mailto:anthony.papavasiliou@uclouvain.be)
- <https://ap-rg.eu/>
- [https://perso.uclouvain.be/anthony.papavasiliou/public\\_html/](https://perso.uclouvain.be/anthony.papavasiliou/public_html/)

- Default design: imbalance penalty  $\alpha$  of Eq. (1) is equal to zero
- Balancing price equals the imbalance price,  $\lambda^I = \lambda^B$
- Compatible with EBGL
- Failure to generate a forward reserve price signal

# Imbalance Penalties (D2)

- Belgian government claims that the imbalance penalty  $\alpha$  “already exhibits quite some characteristics of a scarcity pricing mechanism”
- In case of independent imbalances and a symmetric imbalance penalty  $\alpha$ , design (D2) is shown to behave identically to design (D1)
- Design (D2) relies on imbalance penalties  $\alpha$  which depend on level of system imbalance, not to be confused with level of scarcity in the system
- In practice, imbalance  $\alpha$  depends on imbalance of the current and previous interval  $\Rightarrow$  MDP model requires an additional state variable, imbalance of previous balancing interval (added to state vector of stages 2 and 3)

- ORDC adder:

$$\lambda^R = (VOLL - \lambda^B) \cdot LOLP(P^{+,tot} - Imb^t) \cdot \mathbb{I}[P^{+,tot} - Imb^t \geq 0] + (VOLL - C^{max}) \cdot \mathbb{I}[P^{+,tot} - Imb^t < 0] \quad (1)$$

- $VOLL$ : estimate of value of lost load
- $P^{+,tot}$ : total reserve capacity
- $LOLP(\cdot)$ : loss of load probability as a function of available reserve capacity
- $C^{max}$ : estimate of marginal cost of marginal unit
- ELIA proposal: apply  $\lambda^R$  as an imbalance charge
- This produces a forward reserve price that is significantly weaker than the average value of balancing capacity to the system

# Scarcity Pricing (D4)

- Replace  $\alpha$  with  $\lambda^R$  in Eq. (1)
- Introduce the following term in settlement:

$$-\lambda^R \cdot qa^R + \lambda^R \cdot (P^+ - qa - ai)$$

- Second term induces agents to bid reserve capacity in forward markets in a way that anticipates expected price at which they would be required to buy that reserve capacity back in real time  $\Rightarrow$  **back-propagation**
- D4 implements an imbalance mechanism for balancing capacity / RT market for reserve capacity (analogous to imbalance mechanism for balancing energy / RT energy market)
- Compatible with article 20 of Clean Energy Package
- We need to add awarded day-ahead reserve capacity  $qa^R$  to state of third time step of MDP model (since it affects third-stage payoff)

Fringe agent that we are interested in is agent A5

	A1	A2	A3	A4	A5	A6	A7	A8
$P^+$	0	0	0	0	1	100	100	100
$P^-$	-100	-100	-100	-50	0	0	0	0
$C$	20	30	40	50	50	60	70	80

**Table:** Units are in [MW] for  $P^+$  and  $P^-$ , and in [€/MWh] for  $C$ .

- For design ( $D2$ ), we use ELIA formula:  $UI = LI = 150$  MW, and

$$\alpha^U = \alpha^L = \frac{200}{1 + \exp\left(\frac{450-x}{65}\right)}$$

where  $x = \frac{|Imb^t| + |Imb_{t-1}^t|}{2}$  is the average of the absolute total system imbalances of the previous and current imbalance interval

- For design ( $D3$ ) and ( $D4$ ), we assume  $VOLL = 920$  €/MWh
- Q-learning algorithm
  - Learning rate:  $\frac{1}{n(s,a)}$  for each state-action pair ( $s, a$ ), where  $n(s, a)$  counts the number of visits to ( $s, a$ )
  - We run 2,000,000 episodes for each design with the same seeds, in order to isolate the effect of the market design changes on the results

Design	(D1)	(D2)	(D3)	(D4)
$q^*$ [MW]	1	1	0	1
$p^*$ [€/MWh]	50	50	any	50
Average Profit [€]	4.04	4.04	12.57	16.63
Opportunity cost $dR^*/dq$ [€]	0	0	8.53	12.59

Table: Analytical Solution

Design	(D1)	(D3)	(D4)
$q^*$ [MW]	1	0	1
$p^*$ [€/MWh]	55	any	50
Average Profit [€]	6.34	14.43	18.85
Opportunity cost $dR^*/dq$ [€/MWh]	0	8.11	12.71

Table: MDP results for (D1), (D3) and (D4)

$Imb_{t-1}^t$ [MWh]	$(\infty, -150]$	$(-150, 0]$	$(0, 150]$	$(150, \infty)$
$q^*$ [MW]	1	1	1	1
$p^*$ [€/MWh]	50	55	55	50
Average Profit [€]	6.43	6.30	6.32	6.46
$dR^*/dq$ [€/MWh]	0	0	0	0

Table: MDP results for (D2)

- For every design, the bid quantity and price are equivalent for the analytical case and the MDP model
- Profits are in the same range for the analytical solution and the MDP model
- Opportunity costs are very close to each other for the analytical model and the MDP code
- For design ( $D2$ ), the range of values in the imbalance of the previous period,  $Imb_{t-1}^t$ , does not influence the selected action or the profit, in line with analytical results