# Multi-Area Stochastic Unit Commitment for High Wind Penetration in a Transmission Constrained Network

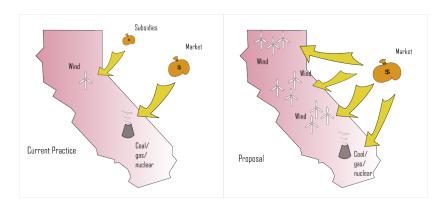
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November 1, 2015



# A Vision for Renewable Energy



Renewable resources can become economically competitive by targeting flexible consumers



## Research Objective

In order to assess the economic implications of large-scale renewable integration, we seek to quantify:

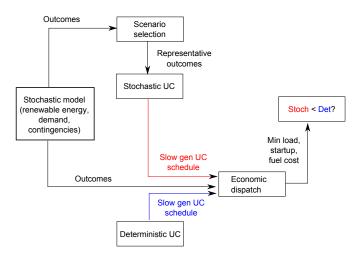
- Renewable energy utilization
- Cost of unit commitment and economic dispatch
- Capital investment in generation capacity

Stochastic unit commitment an appropriate model:

- Quantifies renewable energy utilization (decision variable)
- Quantifies operating costs (objective function)
- Endogenously determines reserves (as opposed to ad hoc rules)



### Validation of Stochastic Unit Commitment Model



## Unit Commitment and Economic Dispatch

- Deterministic model (Sioshansi and Short, 2009)
  - Reserve requirements

$$\sum_{g \in G} s_{gt} + \sum_{g \in G_f} f_{gt} \geq T_t^{\text{req}}, \sum_{g \in G_f} f_{gt} \geq F_t^{\text{req}}, t \in T$$

Import constraints

$$\sum_{l \in IG_j} \gamma_{jl} e_{lt} \leq IC_j, j \in \mathcal{IG}, t \in T$$

• Slow generator schedules are fixed in economic dispatch model:  $w_{gt} = w_{gt}^{\star}, g \in G_s$ 



### Two-Stage Stochastic Unit Commitment

- In the first stage we commit slow generators:  $u_{gst} = w_{gt}, v_{gst} = z_{gt}, g \in G_s, s \in S, t \in T$  (corresponds to day-ahead market)
- Uncertainty is revealed: net demand  $D_{nst}$ , line availability  $B_{ls}$ , generator availability  $P_{gs}^+$ ,  $P_{gs}^-$
- **③** Fast generator commitment and production schedules are second stage decisions:  $u_{gst}$ ,  $g ∈ G_f$  and  $p_{gst}$ ,  $g ∈ G_f ∪ G_s$  (corresponds to real-time market)
- Objective:

$$\min \sum_{g \in G} \sum_{s \in S} \sum_{t \in T} \pi_s (K_g u_{gst} + S_g v_{gst} + C_g p_{gst})$$



## Lagrangian Decomposition Algorithm

- Past work: (Takriti et al., 1996), (Carpentier et al., 1996), (Nowak and Römisch, 2000), (Shiina and Birge, 2004)
- Key idea: relax non-anticipativity constraints on both unit commitment and startup variables
  - Balance size of subproblems
  - Obtain lower and upper bounds at each iteration

#### Lagrangian:

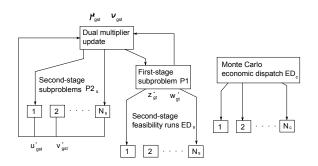
$$\mathcal{L} = \sum_{g \in G} \sum_{s \in S} \sum_{t \in T} \pi_s (K_g u_{gst} + S_g v_{gst} + C_g p_{gst})$$

$$+ \sum_{g \in G_s} \sum_{s \in S} \sum_{t \in T} \pi_s (\mu_{gst} (u_{gst} - w_{gt}) + \nu_{gst} (v_{gst} - z_{gt}))$$



### **Parallelization**

- Second-stage subproblems, second-stage feasibility runs and economic dispatch simulations can be parallelized
- Implemented in MPI, CPLEX

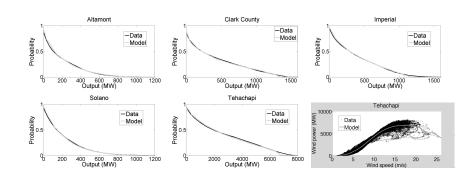


# Scenario Selection for Wind Uncertainty and Contingencies

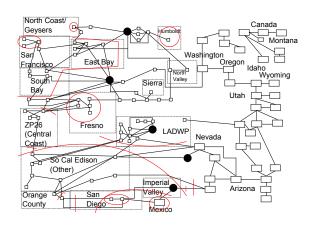
- Past work: (Gröwe-Kuska et al., 2002), (Dupacova et al., 2003), (Heitsch and Römisch, 2003), (Morales et al., 2009)
- Scenario selection algorithm inspired by importance sampling
  - Generate a sample set  $\Omega_S \subset \Omega$ , where  $M = |\Omega_S|$  is adequately large. Calculate the cost  $C_D(\omega)$  of each sample  $\omega \in \Omega_S$  against the best determinstic unit commitment
    - policy and the average cost  $\bar{C} = \sum_{i=1}^{M} \frac{C_D(\omega_i)}{M}$ .
  - ② Choose N scenarios from  $\Omega_S$ , where the probability of picking a scenario  $\omega$  is  $C_D(\omega)/\bar{C}$ .
  - 3 Set  $\pi_s = C_D(\omega)^{-1}$  for all  $\omega^s \in \hat{\Omega}$ .



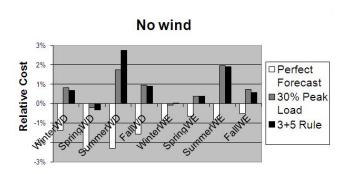
### Multi-Area Wind Model



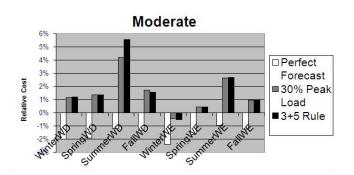
### **WECC Model**



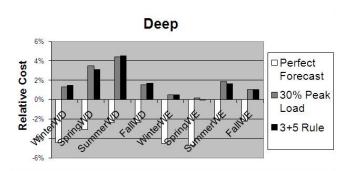
# Policy Comparison - No Wind Integration



# Policy Comparison - Moderate Integration



## Policy Comparison - Deep Integration



# Summary

	Deep-S	No Wind	Moderate	Deep
RE daily waste (MWh)	100	0	890	2,186
Cost (\$M)	5.012	11.508	9.363	7.481
Capacity (MW)	20,744	26,377	26,068	26,068
Daily savings (\$)	38,628	104,321	198,199	188,735
Forecast gains (%)	32.4	35.4	41.9	46.7

## Conclusions and Perspectives

- Consistent performance of scenario selection:
   Stochastic unit commitment policy yields 32.4% 46.7% of potential benefits of perfect foresight over various types of uncertainty
- Transmission constraints and contingencies strongly influence results - need for advanced optimization
  - Overestimation of capacity credit from 1.2% of installed wind capacity to 39.8% for deep integration
  - Underestimation of daily operating costs from 7.481 \$M to 5.102 \$M for deep integration
- New frontiers for renewable integration studies
  - Sub-hourly resolution and ramp rates
  - Detailed models of system resources (demand response, CCGTs, nuclear, hydro)
  - Parallel computing

