Introduction

Quantitative Energy Economics

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Motivation

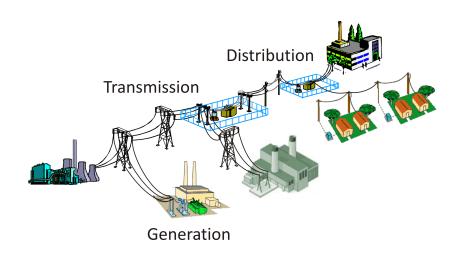
Organization of Material

Paradigm Shift

Operations research more important than ever in energy

- Policy changes
 - Deregulation
 - Renewable energy integration
- Technology changes
 - Evolution of solvers
 - Parallel computing

Electricity Supply Chain



The integrated operation of the electricity supply chain ...

Deregulation

... has been replaced by a market



Electricity price in Belgium, January 18-25, 2015

Renewables Making Headlines





Denmark aims for 100 percent renewable energy in 2050

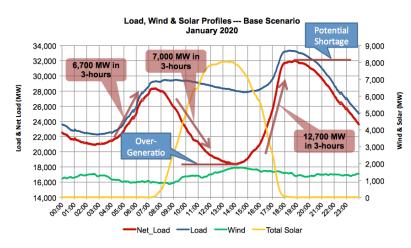
BY METTE FRAENDE

COPENHAGEN | Fri Nov 25, 2011 11:49am EST



California to nearly double wind, solar energy output by 2020 -regulator

The Duck Chart



Net Load = Load - Wind - Solar

Evolution of Solvers



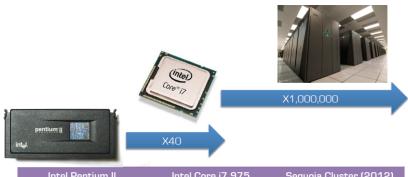


In 1952, Dantzig et al. solve an instance of the Traveling Salesman Problem with 49 cities **by hand**

In 2006 Cook et al. solve a problem with 85,900 'cities' [the one above has 37,000 cities]

lt took	lt takes
> 4 months (early 90's)	1 second (2007)
> 7 years (early 90's)	1 second (now)

Parallel Computing



Intel Pentium II (1997-1999)	Intel Core i7 975 (2014)	Sequoia Cluster (2012)
233-450 MHz	3.33 GHz	PowerPC A2 2.3 GHz
1 core	4 cores	1.6 million cores

Operations Research in the Energy Industry

The energy industry is a very active user of OR

- Late 1980s: Lagrange relaxation applied in unit commitment
- Early 2000s: adoption of branch-and-bound in unit commitment, MISO reports \$2.1 - \$3 billion savings between 2007 and 2010!
- Late 1980s: stochastic dual dynamic programming solves medium-term hydrothermal scheduling, used in most hydrothermal systems today to determine water levels and prices (Brazil, Scandinavia, Turkey, Switzerland)

Example: PJM Day-Ahead Market Model



Day-ahead Market – Average Daily Volumes

- 1,210 generators, 3 part offers (startup, no load, 10 segment incremental energy offer curve)
- 10,000 Demand bids fixed or price sensitive
- 50,000 Virtual bids / offers
- 8,700 eligible bid/offer nodes (pricing nodes)
- 6,125 monitored transmission elements
- 10,000 transmission contingencies modeled
- Solved by mixed integer linear programming
- PJM traded \$50.03 billion (!) in 2014



Learning Outcomes

- Explain the architecture of electricity markets
- Formulate math programs that describe energy markets and regulations
- Formulate math programs that describe risk management
- Implement models using AMPL

Topics

- Mathematical background
- Power system operations
- Power market operations
- Economic dispatch, competitive market equilibrium
- The transmission network
- Ancillary services
- Unit commitment
- Financial instruments
- Demand response
- Capacity expansion